

Reporting uncertainty

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Dr. C. H. Meyers, reporting on his measurements of the heat capacity of ammonia:

We think our reported value is good to 1 part in 10000:

we are willing to bet our own money at even odds that it is correct to 2 parts in 10000.

Furthermore, if by any chance our value is shown to be in error by more than 1 part in 1000, we are prepared to eat the apparatus and drink the ammonia!

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Err on the side of providing more information

- Describe methods used to calculate result and uncertainty
- List all uncertainty components and how they were evaluated
- Present data analysis so that independent calculation can be repeated
- give all corrections and constants used and their sources

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When using $u_c(y)$...

- In one of the 4 following ways
- " $m_s=100.02147g$ with (a combined standard uncertainty) $u_c=0.35mg$ "
- " $m_s=100.02147(35)g$, where the number in parentheses is the numerical value of (the combined standard uncertainty) u_c referred to the corresponding last digits of the quoted result." ↓

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When using $u_c(y)$...

- " $m_s=100.02147(0.00035)g$, where the number in parentheses is the numerical value of (the combined standard uncertainty) u_c expressed in the unit of the quoted result."
- " $m_s=(100.02147\pm 0.00035)g$, where the number following the symbol \pm is the numerical value of (the combined standard uncertainty) u_c and not a confidence interval" ↓

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When using U

- " $m_s=(100.02147\pm 0.00079)g$, where the number following the symbol \pm is the numerical value of (an expanded uncertainty) $u_c=0.35mg$ and (a coverage factor) $k=2.26$ based on the t distribution for $\nu=9$ degrees of freedom, and defines an interval estimated to have a level of confidence of 95 percent." ↓

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Number of digits...

- Do not give excessive number of digits
- At most two digits, but sometimes more may be required to avoid round off errors in subsequent calculations
- Round up, in general
- $u_c(y)=10.47\text{m}\Omega$ might be rounded to $11\text{m}\Omega$
- But use common sense
- $u_c(y)=28.05\text{kHz}$ maybe rounded to 28kHz ↓

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Number of digits...

- Round off measurement result to be consistent with their uncertainties
- If $y=10.05762\Omega$ with $u_c(y)=27\text{m}\Omega$,
- y should be rounded to 10.058Ω
- Correlation coefficients should be given with three digit accuracy if their absolute values are near unity ↓

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Detailed report...

- Give each input estimate and its standard uncertainty
- Give estimated covariances or correlation coefficients associated with correlated input estimates
- Give degrees of freedom for the standard uncertainty of each input
- Give the functional relationship, sensitivity coefficients ↓↓

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