## PE255T 2008 Metrology and Computer Aided Inspection – Test 1

1. What are the various elements of a measurement system? Identify these elements for a Bourden tube type pressure gauge. (2 marks) 2. A standard resistance of 100ohms was measured using two different multimeters A & B with the following results: A) 101, 102, 98, 99, 104, 103, 95, 103, 95, 97 and B) 100, 102, 101, 99, 102, 103, 100, 99, 104, 100. Which multimeter is more accurate? Which is more precise? Justify your answer. (2 marks) 3. Define a) influence quantity b) metrological traceability. (2 marks) 4. Explain the evolution in the definition of the "metre". (2 marks) 5. The temperature inside a room was measured at six different places as 28, 31, 30, 29, 28, 30. Determine a 95% expanded uncertainty interval for the temperature. (2 marks) 6. The resistance of two coils was measured using a multimeter and the results obtained as  $100\Omega$  and  $50\Omega$  with standard uncertainties  $1\Omega$  and  $0.5\Omega$  respectively. Determine the overall resistance and its standard uncertainty if these resistances are connected in parallel. (5 marks)

7. The width of a wooden table was measured as 47cm using a metre scale with least count 1cm and a uniformly distributed uncertainty between divisions. The scale during calibration had shown a zero error +1cm with expanded uncertainty +/-0.5cm (95%). The two uncertainties are estimated to have a correlation of 0.8. Estimate the width of the table and its standard uncertainty. Neglect other sources of uncertainty.

(5 marks)

Max. Marks: 20

Time: 50 minutes

## SOLUTIONS TO MUMERICAL PROBLEMS:

|         | А        | В        |
|---------|----------|----------|
|         | 101      | 100      |
|         | 102      | 102      |
|         | 98       | 101      |
|         | 99       | 99       |
|         | 104      | 102      |
|         | 103      | 103      |
|         | 95       | 100      |
|         | 103      | 99       |
|         | 95       | 104      |
| _       | 97       | 100      |
| Average | 99.7     | 101      |
| Range   | 9        | 5        |
| Stdev   | 3.368151 | 1.699673 |

A is more accurate while B is more precise 5.

|         | 28       |
|---------|----------|
|         | 31       |
|         | 30       |
|         | 29       |
|         | 28       |
|         | 30       |
| average | 29.33333 |
| stdev   | 1.21106  |
| u       | 0.494413 |
| t       | 2.57     |
| U+      | 30.60398 |
| U-      | 28.06269 |

$$R = \frac{R_1 R_2}{R_1 + R_2} = \frac{100 * 50}{100 + 50} = 33.33$$

$$c_{R_1} = \frac{R_2}{R_1 + R_2} - \frac{R_1 R_2}{(R_1 + R_2)^2} = \frac{50}{100 + 50} - \frac{100 * 50}{(100 + 50)^2} = 0.1111$$

$$c_{R_2} = \frac{R_1}{R_1 + R_2} - \frac{R_1 R_2}{(R_1 + R_2)^2} = \frac{100}{100 + 50} - \frac{100 * 50}{(100 + 50)^2} = 0.2222$$
Quantity Result Std sensitivity Contrib
Uncertainty
R1 100 1 0.111111 0.111111
R2 50 0.5
R 33.3333 0.248456

| Numerical a | approach: |             |          |          |          |          |
|-------------|-----------|-------------|----------|----------|----------|----------|
| Quantity    | Result    | Std         | R1+      | R1-      | R2+      | R2-      |
|             |           | Uncertainty |          |          |          |          |
| R1          | 100       | 1           | 101      | 99       | 100      | 100      |
| R2          | 50        | 0.5         | 50       | 50       | 50.5     | 49.5     |
| R           | 33.33333  | i           | 33.44371 | 33.22148 | 33.55482 | 33.11037 |
|             |           |             | 0.111116 |          | 0.222225 |          |
|             |           |             | 0.061731 |          |          |          |
|             |           |             | 0.248456 | -        |          |          |

7.  
L = M - E = 47 - 1 = 46cm  

$$u(M) = \frac{0.5}{\sqrt{3}} = 0.288675; u(E) = \frac{0.5}{1.96} = 0.25510;$$

$$c_M = 1; c_E = -1$$
  
 $u_c = \sqrt{0.288675^2 + (-0.25510)^2 - 0.11783} = 0.174882$ 

Numerical approach:

| Quantity | Result | e e | Std         | M+       | M-       | E+       | E-       |          |
|----------|--------|-----|-------------|----------|----------|----------|----------|----------|
| -        |        | ι   | Jncertainty |          |          |          |          |          |
| Μ        |        | 47  | 0.288675    | 47.28868 | 46.71132 | 47       | 47       |          |
| E        |        | 1   | 0.255102    | 1        | 1        | 1.255102 | 0.744898 |          |
| L        |        | 46  |             | 46.28868 | 45.71132 | 45.7449  | 46.2551  |          |
|          |        |     |             | 0.288675 |          | -0.2551  |          | -0.11783 |
|          |        |     | 0.030584    |          |          |          |          |          |
|          |        |     | 0.174882    | -        |          |          |          |          |
|          |        | _   |             |          |          |          |          |          |